# Evaluation of accurate eye corner detection methods for gaze estimation

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Low cost eye tracking based on simple hardware such as web cams faces new obstacles for researchers working in the field. Creating new strategies for gaze estimation is one of the most challenging tasks. If no infrared light sources are employed the image quality decreases considerably and makes it difficult to use the pupil center as tracking feature. Accurate detection of iris center and eye corners appears to be a promising approach for low cost gaze estimation. Since iris detection has been covered by previous works, in this paper we propose novel eye inner corner detection methods. Appearance and feature based segmentation approaches are suggested. All these methods are exhaustively tested on a realistic dataset containing images of subjects gazing at different points on a screen. The results show promising conclusions regarding the use of these methods in real low cost eye tracking systems. **Keywords: eye tracking, low cost, eye inner corner** 

## Introduction

Research on eye detection and tracking has attracted much attention in the last decades. Since it is one of the most stable and representative features of the subject, eye detection is used in a great variety of applications, such as subject identification, human computer interaction as shown in Morimoto and Mimica (2005) and gesture recognition as described by Tian, Kanade, and Cohn (2000) and Bailenson et al. (2008).

Human computer interaction based on eye information is one of the most challenging research topics in the recent years. According to the literature, the first attempts to track the human gaze using cameras began in 1974 as shown in the work by Merchant, Morrissette, and Porterfield (1974). Since then, and especially in the last decades, much effort has been devoted to improving the performance of eye tracking systems. The availability of high performance eye tracking systems has provided advances in fields such as usability research as described by Ellis, Candrea, Misner, Craig, and Lankford (1998) Poole and Ball (2005) and interaction for severely disabled people in works such as Bolt (1982), Starker and Bolt (1990) and Vertegaal (1999). Gaze tracking systems can be used to determine the fixation point of an individual on a computer screen, which can in turn be used as a pointer to interact with the computer. Thus, severely disabled people who cannot communicate with their environment using alternative interaction tools can perform several tasks by means of their gaze. Performance limitations, such as head movement constraints, limit the employment of the gaze trackers as interaction tools in other areas. Moreover, the limited market for eye tracking systems and the specialized hardware they employ, increase their prices. The eye tracking community has identified new application fields, such as video games or the automotive industry, as potential markets for the technology (Zhang, Bulling, & Gellersen, 2013). However, simpler (i.e., lower cost) hardware is needed to reach these areas.

Although web cams offer acceptable resolutions for eye tracking purposes, the optics used provide a wider field of view in which the whole face appears. By contrast, most of the existing high-performance eye tracking systems employ infrared illumination. Infrared light-emitting diodes provide a higher image quality and produce bright pixels in the image from infrared light reflections on the cornea named as glints. Although some works suggest the combination of light sources and web cams to track the eyes as described in Sigut and Sidha (2011), the challenge of low-cost systems is to avoid the use of light sources to keep the systems as simple as possible; hence, the image quality decreases. High-performance eye tracking systems usually combine glints and pupil information to compute the gaze position on the screen. Accurate pupil detection is not feasible in web cam images, and most works on this topic focus on iris center. In order to improve accuracy, other elements such as eye corners or head

position are necessary for gaze estimation applications, apart from the estimation of both irises. In the work by Ince and Yang (2009), they consider that the horizontal and vertical deviation of eye movements through eyeball size is directly proportional to the deviation of cursor movements in a certain screen size and resolution. Fukuda, Morimoto, and Yamana (2010) employ iris information and eyeball geometry information in their gaze estimation method. Other approaches use preprocessed eye regions to train a neural network as made by Sewell and Komogortsev (2010). If user movement tolerance is required, as well as iris position, head position is needed. Using eye corners is a straightforward method to overcome this problem, and the corners are employed in several works to improve gaze estimation accuracy as it is shown in Valenti, Staiano, Sebe, and Gevers (2009) and in Sesma, Villanueva, and Cabeza (2012). The work by Zhu and Yang (2002) presents a web cam based eye tracking system. Although it uses infrared for image processing purposes, the relevant aspect of their paper is that they use iris and corner information for gaze estimation.

Compared to other facial features detection methods accuracy is key for gaze estimation purposes. Recently, several papers have been presented about accurate iris center detection using a web cam as shown in Timm and Barth (2011) and Villanueva et al. (2013), however, not much has been published about accurate eye corner detection. Regarding eye corner estimation, we find works in which corners are detected as a result of facial features detection methods. Recently, Dibeklioglu, Salah, and Gevers (2011) and Belhumeur, Jacobs, Kriegman, and Kumar (2011) have presented relevant works in the area. In the same manner, works in which a specific detection of the eye corner is carried out have been presented lately. In Zhu and Yang (2002), they present a method based on spatial filtering and corner shape masks to detect eye corners. Zhou, He, Wu, Hu, and Meng (2011) use Harris detector and texture analysis to determine eye corners in the image. Haiying and Guoping (2009) apply weighted variance projection function to determine a rough corner area and Harris corner detector to improve the accuracy. However, none of this methods present the require accuracy for gaze estimation purposes.

In this paper, we propose a group of novel eye inner corner detection methods providing higher accuracies. In our previous work Villanueva et al. (2013), we suggested a method to detect the outer corner of the eye. However, recent experiments show that the inner corner shape is more robust and stable. Thus, we propose new methods for this corner detection. On the one hand, we adapt well-known appearance based segmentation methods for corner detection and on the other hand we use improved techniques for feature detection and eye corner segmentation.

This paper is organized as follows. In the next section appearance based segmentation methods are pre-



*Figure 1.* The points shown in the figure are the alternative landmarks that have to be placed by the expert in the eye area.



*Figure 2.* One of the training images in which the ASM model is overlapped.

sented. To follow, features detection methods are described together with the initialization strategy employed. Finally, the experiments carried out and the results are presented.

## Appearance based methods

Active Shape Models (ASM) and Active Appearance Models (AAM) methods have been largely used for segmentation of facial features. These detection techniques were introduced by Cootes, Edwards, and Taylor (2001) and Cootes, Taylor, Cooper, and Graham (1995) and are based on a previous learning procedure in which an expert marks key segmentation points in images from a training set. If the variety of the training examples is sufficiently broad in order to capture the possible forms (shape and texture) of the object(s) to segment, these techniques will be able to segment new instances of the same object in images not contained in the training set. Both techniques study the statistical behavior of the object to be segmented in terms of shape, appearance and texture. This study is performed based on the segmentation points placed by the expert during the training stage named as landmarks. ASM segmentation method learns the possible shapes of an object and the appearance of the landmarks while AAM is able to learn textures of the object in addition to the shape. In this paper, we have tested a variety of models based on ASM and AAM in order to detect the eye inner corner. The objective is to segment a facial characteristic, e.g. eye contour, that includes the eye inner corner as landmark. Thus, once the whole facial feature is segmented the landmark of the model corresponding to the eye inner corner is provided as result.

The first two methods proposed try to model the area containing both eyes. The employed landmarks are shown in figure 1. The first method is based on ASM and tries to model the behavior of the shape shown in figure 2. The model contains both eyes and



*Figure 3.* One of the training images in which the AAM model is overlapped.

landmarks number 9 and 25 are the ones corresponding to the inner corner of both eyes. We refer the reader to the paper Cootes et al. (1995) including more details about the implementation used for the segmentation.

The second method modelling the eye area is based on AAM. The facial area modelled is shown in figure 3. Once the landmarks have been established AAM is able to model the texture of the object areas contained in the triangles shown in the figure that are constructed using the landmarks as reference.

Both ASM and AAM models have been trained using 83 images of different subjects gazing at alternative points on the screen. One of the weaknesses of ASM and AAM is their sensitivity to the initialization. The model obtained from the training stage needs to be placed close to the real contour of the new instance of the object. If the initialization is appropriate, the model is adapted to the shape of the object in the image by means of an iterative procedure that modifies the location of the landmarks according to the learnt model. Both methods, i.e. ASM and AAM, are initialized using the position of the iris centers of the eyes. Once the position of the iris is known as described in Villanueva et al. (2013), its position in the image is used to initialize the model.

#### Feature detection methods

Two methods are proposed in order to detect eye inner corner. The first method is based on Harris corner detection and the second method uses Canny edge detection in order to detect the eyelid. Both methods are applied in a previously estimated searching area in which the eye corner is contained. The detection of this region of interest is explained first.

In order to establish this searching area alternative methods have been tested. Using the irises of the eye is one of the evaluated options, i.e. selecting a window between the iris center and the nose. However, it presents a low robustness since the iris center position can vary as a function of gaze direction.

The method proposed is a multi-stage procedure in which the face is previously segmented using Viola-Jones face detector. The segmentation provides a rectangle in which the face is contained. Thus, the eye area is segmented assuming that the eyes will be contained in the upper part of the face. Left and right eyes areas are obtained by dividing the eye area in two parts. A neural network has been trained to detect the eye inner corner area (in the previously segmented eye areas). The network employed is a feed-forward back propagation network with one hidden layer. We use RGB patches with size 7x7 of the eye area to train the neural network. In order to achieve the best results, we train the network using more negative than positive examples of the eye area, thus, we employ 20% more negative than positive examples.

Once the neural network has been trained it is applied in the eye area. For each one of the methods proposed requiring to be initialized the neural network provides a reduced searching area with more that 90% of certainty.

The Harris corner detector is a popular interest point detector due to its strong invariance to rotation, scale, illumination variation and image noise. The Harris corner detector measures the local changes of the signal with patches shifted by a small amount in different directions. The aim is to find little patches of the image that generate a large variation when moved around. Given a pixel and its neighborhood a matrix *M* can be calculated as:

$$M = \begin{pmatrix} I_x^2 & I_x I_y \\ I_x I_y & I_y^2 \end{pmatrix}$$
(1)

where,  $I_x$  and  $I_y$  are the derivatives of the image in x and y directions. A score R can be calculated for each point given as:

$$R = det(M) - k * trace(M)$$
<sup>(2)</sup>

where  $det(M) = \lambda_1 \lambda_2$  and  $trace(M) = \lambda_1 + \lambda_2$  and  $\lambda_1$  and  $\lambda_2$  are the eigenvalues of matrix *M*.

The method proposed applies a modified version of the Harris corner detector in the previously detected searching area. The Harris corner detector is applied in the original window and in a smoothed version of the same window with k = 0.06. The searching subimage is smoothed using a Gaussian filter. According to the size of our test images, the filter size is 19x19 and  $\sigma = 4$ . In the original window all the local maxima of the score R are detected as candidates, while a threshold is established in the smoothed image in order to classify it as a candidate. This threshold has been fixed as 50% of the maximum value of R. As expected, less corners are detected in the smoothed version of the image (see figure 4). From our experience in our test images the number of images in which more than one corner are detected (the maximum is two) is negligible in comparison to the total number of images tested. Nevertheless, in those cases the candidate closer to the nose is selected as the best approximation of the corner in the smoothed image.

In the original searching window the Harris detector segments all local maxima as corner candidates. The number of candidates makes it difficult to select the one corresponding to the inner corner. However, the detections present higher accuracy especially if this is com-



*Figure 4.* Given the whole image the eye area and the searching window are previously segmented. Once the searching area is applied the eye inner corner is calculated as the corner obtained in high resolution image (cross) closer to the corner obtained in the lower resolution image (asterisk).

pared with the one obtained in the smoothed version of the image.

The method proposed combines the detections obtained in the original and smoothed versions of the searching window. Thus, the inner corner is selected as the candidate in the original window closer to the one obtained in the smoothed image. In this manner, the accuracy obtained in the original window is combined with the predictive ability of the Harris method in the low resolution version of the image.

The second method proposed combines two well known techniques to detect the inner corner of the eye. It combines an edge detection method and topography to determine the eye inner corner. The searching area is also previously calculated as it has been previously described in this section. In the searching area we use a Canny edge detector to segment the upper eyelid. For the test images  $\sigma=2$  is used. In addition, since the upper eyelid has a stronger horizontal component only the corresponding component of the Canny detector is used, i.e. the horizontal component. Once the edge detection is performed, we apply an algorithm to detect curves, which basically fills gaps between edge segments to reconstruct the curve. We consider that two edge segments belong to the same curve when their distance is one pixel. Thus, the point of this curve closer to the nose is considered to be a good approximation of the eye inner corner (see figure 5). Our experience shows that the detection of this point is robust but it only approximates the real position of the eye inner corner. The main reason for that is the fact that in most of the cases the eyelid is not completely segmented. Nevertheless, it is assumed that this point is a good approximation of the eye inner corner.

In order to improve the accuracy of the method we introduce pit detection. From image topography theory perspective, image pixels can be labeled according to their grey level and the intensity of their neighbouring pixels (Wang, Yin, & Moore, 2007). Given the image f(x,y), the labeling process is performed using the Hessian matrix eigenvalues and the gradient vector behavior. Given a pixel at position (x, y) the Hessian matrix is calculated as:



*Figure 5.* The method based on Canny edge detector is shown. The upper eyelid is previously segmented and the pits in the area are calculated (white dots). The pit selected as the eye inner corner is the one closer to the end point of the eyelid.

$$\mathbf{H}(x,y) = \begin{pmatrix} \frac{\partial^2 f(x,y)}{\partial x^2} & \frac{\partial^2 f(x,y)}{\partial x \partial y} \\ \frac{\partial^2 f(x,y)}{\partial x \partial y} & \frac{\partial^2 f(x,y)}{\partial y^2} \end{pmatrix}$$
(3)

From the eigenvalue decomposition of **H**,  $\lambda_1$  and  $\lambda_2$  eigenvalues are obtained. Differentiation filters based on Chebyshev polynomials are used to approximate topographic labels computation defined for continuous functions to discrete signals (Meer & Weiss, 1992). Image topography allows the labeling of pixels as ridge and pits among others. Thus, the eye corner can be considered to be a valley since, ideally, intensity increases in all directions. In topography, these points are called a "pit". A pixel is classified as a "pit" if the following conditions are satisfied:

$$\|\nabla f(x, y)\| = 0, \lambda_1 > 0, \lambda_2 > 0 \tag{4}$$

According to our results, the eye corner is classified as a pit under image topography perspective. The advantage of topography compared to eyelid segmentation is its accuracy. Thus, we select as inner corner the pit closer to the end point of the eyelid segmented previously.

## Experiments

We have tested four algorithms over images taken from the proprietary Gi4E dataset. The database has been created at the Public University of Navarra and is publicly available (by contacting the authors). This dataset contains images from 100 subjects gazing at different points in the screen. We have selected 200 images from the database arbitrarily. In these images the inner corner has been re-marked by two experts more accurately. The error of the algorithms is calculated as the distance between the estimated inner corner position and the real position as provided in the label. This error is normalized with respect to the distance between the irises of the eye.

$$e = \frac{\| corner_{est} - corner_{label} \|}{iris_{distance}}$$
(5)

The following graph in figure 6 shows the cumulative error for each one of the algorithms, i.e. the horizontal axis indicates error values, i.e. *e*, and the vertical



*Figure 6.* The horizontal axis shows the normalized error of eye inner corner estimation while the vertical shows the performance for each one of the methods. The performance is measured as the percentage of images below certain error value.

one the percentage of images for which the error in the corner detection is below that error threshold e.

From figure 6 it can be observed that the methods based on AAM and Harris corner detector present the best performances. From our experience error value of 0.05 can be acceptable for iris center detection. In this case, all the methods proposed are above 80% of performance, i.e. the 80% of the images present errors below 0.05 in the detected corners. However, our results have shown that the accuracy in the eye inner corner is more critical for gaze estimation. If accuracies of 0.01-0.02 are required the difference between AAM and Harris with respect to the other two methods is more significant. While the best two methods remain above 80% the performance of the other two decreases below 50% for error values of 0.02.

Improving the execution times of the techniques is not the objective of this work. The hardware employed and the software coded in Matlab have not been adapted to achieve the best performance in terms of speed. However, we find it appropriate to provide some numbers about the performance of each one of the proposed techniques. As expected, appearance based models present the highest numbers, moreover the execution times of feature detection methods is negligible compared to ASM and AAM. On the other hand, Canny and Harris detectors present a comparable behavior. The execution times of ASM and AAM are 171% and 285%, higher than the ones achieved by feature detection methods. In addition, regarding the Canny and Harris methods the 99% of the execution time is devoted to calculating the searching area employing the neural network. Once the searching window is determined, the time employed by feature detection methods is of milliseconds.

### Conclusions

Low cost gaze estimation using web cams presents new challenges for researchers working in the field. If no infrared light sources are used iris center and eye corners can be considered as valid features for gaze estimation. Most of the algorithms devoted to detecting iris and eye corners lack of the required accuracy for gaze estimation purposes. We propose four novel approaches for eye inner corner accurate detection. Two of the methods proposed are methods based on appearance while the other two are methods for features detection.

The methods have been tested over 200 images in which the eye inner corner has been accurately marked. The results show that there is not a difference between the methods based on appearance and the methods for features detection. In fact, the best two methods are the one based on AAM and the method based on Harris detector. If no additional requirements of the system are provided both methods may be valid. However, the fact that the AAM detector needs a previous training stage can represent a drawback of this method compared to the one based on Harris detector.

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